



UCI CHEM267 – Photochemistry, Spring 2023

234

## Lecture #10 of 12

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235

## Photophysical Processes

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### Today's Critical Guiding Question

236

*What continuity/conservation laws are most important for photophysical processes like absorption and emission of photons... for real this time, again: Part 4?*

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## Photophysical Processes

(UPDATED) 237

- Blackbody radiation, Photon properties, Light–Matter interactions, Conservation laws, **Einstein coefficients**
- Jablonski diagram, Spin multiplicity, Internal conversion, Intersystem crossing, Thexi state, Kasha–Vavilov rule, Stokes shift, PL
- Born–Oppenheimer approximation, Franck–Condon principle, Transition dipole moment operator, Franck–Condon factors, **Beer–Lambert law, Absorption coefficient, Oscillator strength, Absorptance**
- Luminescence processes, **Selection rules, Charge-transfer transitions, Spin–Orbit coupling, Heavy-atom effect, E–k diagrams, Jortner energy gap law, Conical intersections**, Energy transfer, Exciplex/Excimer
- **Photoluminescence spectrometer, Emission/Excitation spectra, Inner filter effects, Anisotropy, Excited-state lifetime, Emission quantum yield**



## Nuclear Terms & F–C Factors

(REVIEW) 238

Turro, Chapters 2 and 3

$$k_{obs} \sim \rho | \langle \Psi_1 | P_{1 \rightarrow 2} | \Psi_2 \rangle |^2 \quad \text{Fermi's golden rule}$$

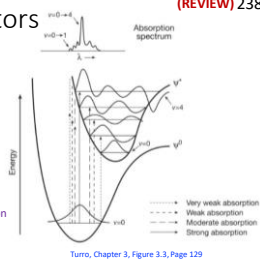
Observed Rate Constant  $k_{obs}$  = Zero-point Motion Limited Rate Constant  $k_{max}^0$  × "Fully Allowed Rate"  $f_{FC} \times f_{SO} \times f_S$

$\Psi \sim \Psi_{el} \chi$   
 ("el") molecular wave function Exact solution to Eq. 2.1  
 ("FC") Franck-Condon factor Approximate solution to Eq. 2.1

... separable due to the Born–Oppenheimer approximation

$$k_{obs} = \left[ \frac{k_{max}^0 \times \langle \psi_1 | P_{1 \rightarrow 2} | \psi_2 \rangle^2}{\Delta E_{12}^2} \right] \times \left[ \frac{\langle \chi_1 | P_{1 \rightarrow 2} | \chi_2 \rangle^2}{\Delta E_{12}^2} \right] \times \left[ \langle \chi_1 | \chi_2 \rangle^2 \right]$$

Overlap integral,  $S_{12} = \int_{-\infty}^{\infty} \chi_1^*(x) \chi_2(x) dx = \langle \chi_1 | \chi_2 \rangle$   
 Franck–Condon factor,  $(\chi_1 | \chi_2)^2$



Transition to what vibronic state is most favorable/rapid by absorption? ... and what about by emission?



## B–O Approximation, F–C Principle, TDM Operator

(REVIEW) 239

- **Born–Oppenheimer (B–O) approximation:** separability of electronic and nuclear terms in the wavefunction

$\Psi \sim \Psi_{el} \chi$   
 ("el") molecular wave function Exact solution to Eq. 2.1  
 ("FC") Franck-Condon factor Approximate solution to Eq. 2.1

- **Franck–Condon (F–C) principle:** Nuclei are fixed during electron-transfer between orbital (*think Libby*)

- **Transition dipole moment (TDM) operator,  $\mu$ :**

$$\mu = \mu_e + \mu_n \Rightarrow \sum_i r_i + \sum_j R_j$$

The probability amplitude  $P$  for the transition between these two states is given by

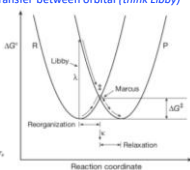
$$P = \langle \psi^1 | \mu | \psi^0 \rangle = \int \psi^1 \mu \psi^0 d\tau, \quad \psi = \psi_e \psi_n$$

$$P = \langle \psi_e^1 \psi_n^1 | \mu | \psi_e^0 \psi_n^0 \rangle = \int \psi_e^1 \psi_n^1 \langle \mu_e + \mu_n | \psi_e^0 \psi_n^0 \rangle d\tau$$

$$= \int \psi_e^1 \psi_n^1 \mu_e \psi_e^0 \psi_n^0 d\tau + \int \psi_e^1 \psi_n^1 \mu_n \psi_e^0 \psi_n^0 d\tau$$

$$= \int \psi_e^1 \psi_n^1 d\tau_e \int \psi_n^1 \mu_e \psi_e^0 d\tau_e \int \psi_e^1 \psi_n^1 d\tau_n = \int \psi_e^1 \psi_n^1 d\tau_e \int \psi_e^0 \psi_n^0 d\tau_n \int \psi_n^1 \mu_n \psi_n^0 d\tau_n$$

Franck–Condon factor    orbital selection rule    selection rule



### Selection Rules

**Angular Momentum Quantum Numbers**

Photon... which came from matter:  $s = 1, m_s = \pm 1$   
 Electron (Orbital):  $l, m_l = [-l, l]$  in steps of 1  
 Electron (Spin):  $s = \frac{1}{2}, m_s = [-\frac{1}{2}, \frac{1}{2}]$

$$= \int \psi_f^* \psi_i d\tau \int \psi_f^* \mu_x \psi_i d\tau \int \psi_f^* \psi_i d\tau$$

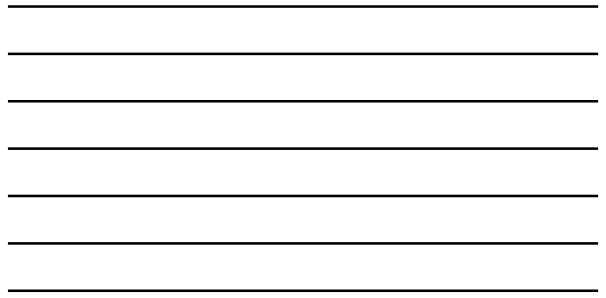
Fracnk-Coulin factor      orbital selection rule      spin selection rule

... well these are just overlaps... and so the more overlap, the more favorable a transition...  
 ... the F-C factor makes sense based on pictures on previous slides  
 ... but what does  $\mu_e$  do to a wavefunction?...  
 ... maybe we don't know, but it better change the angular momentum properly for a photon  
 ... and what are spin wavefunctions?... just symbols!... spin does not appear in  $\mu$ ... it's just math...  
 ... so, the spin wavefunctions only overlap when they are identical... meaning spin does not change

**Atomic Selection "rules"**

Orbital angular momentum (**Laporte "rule"**):  $\Delta l = \pm 1$ ... as  $l_f = l_i \pm s_{\text{photon}}$   
 Spin angular momentum (**Wigner "rule"**):  $\Delta m_s = 0$ ...  $\mu$  does not act on spin  
 Orbital z-direction angular momentum:  $\Delta m_l = 0, \pm 1$ ... as  $m_{l,f} = m_{l,i} \pm m_{s,\text{photon}}$   
 ... the allowed 0 option can be envisioned as two vectors that are opposite in one direction

240



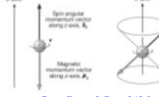
### Selection Rules

| State   | Symbol | $M_L$  | Magnetic Energy ( $\mu_B M_L$ ) | Spin Function               | Spin Representation     |
|---------|--------|--------|---------------------------------|-----------------------------|-------------------------|
| Doublet | $D_1$  | $+1/2$ | $+1/2 \mu_B M_L$                | $\alpha$                    | $\uparrow \downarrow$   |
| Doublet | $D_2$  | $-1/2$ | $-1/2 \mu_B M_L$                | $\beta$                     | $\downarrow \uparrow$   |
| Triplet | $T_3$  | 0      | 0                               | $\alpha\beta - \beta\alpha$ | $\uparrow \uparrow$     |
| Triplet | $T_2$  | $+1$   | $+1 \mu_B M_L$                  | $\alpha\alpha$              | $\uparrow \uparrow$     |
| Triplet | $T_1$  | 0      | 0                               | $\alpha\beta + \beta\alpha$ | $\uparrow \downarrow$   |
| Triplet | $T_0$  | $-1$   | $-1 \mu_B M_L$                  | $\beta\beta$                | $\downarrow \downarrow$ |

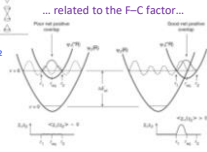
$$= \int \psi_f^* \psi_i d\tau \int \psi_f^* \mu_x \psi_i d\tau \int \psi_f^* \psi_i d\tau$$

Fracnk-Coulin factor      orbital selection rule      spin selection rule

... related to spin-orbital coupling...



Turro, Chapter 2, Figure 2.13, Page 99



... related to the F-C factor...

Turro, Chapter 2, Table 2-4, Page 102

Turro, Chapter 3, Figure 3.5, Page 133

**Summary of Atomic Selection "rules"**

$\Delta l = \pm 1$ ... as  $l_f = l_i \pm s_{\text{photon}}$ ...  $\Delta m_s = 0$ ...  $\Delta m_l = 0, \pm 1$ ... as  $m_{l,f} = m_{l,i} \pm m_{s,\text{photon}}$

**Heavy Molecule (Russell-Saunders L-S Coupling) Selection "rules"**

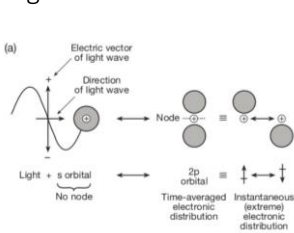
Total angular momentum:  $\Delta J = 0, \pm 1$ ... and  $\Delta S = 0$ ... and  $\Delta L = 0, \pm 1$   
 Total z-direction angular momentum:  $\Delta m_J = 0, \pm 1$ ... and 0's are there for the same reason

241

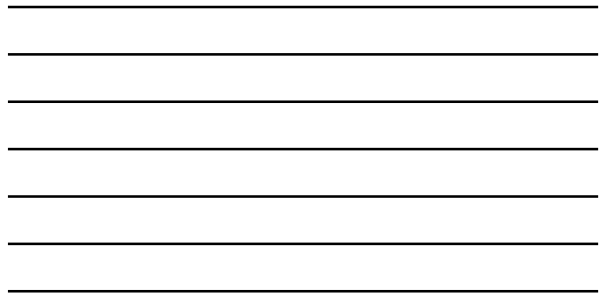
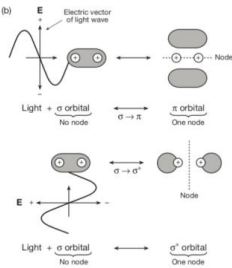


### Light-Matter Interactions

(REVIEW) 242



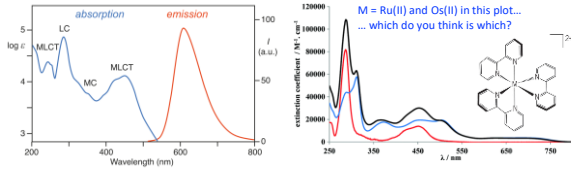
Turro, Chapter 4, Figure 4.6, Page 189



## Charge-Transfer Transitions & S–O Coupling 243

The Hamiltonian for spin-orbit (S–O) coupling results in the **heavy-atom effect**...  
 ... and it also results in variation in the selection rules...  
 Total angular momentum:  $\Delta J = 0, \pm 1$   
 Total z-direction angular momentum:  $\Delta m_j = 0, \pm 1$

$$E_{SO} = Z^4 \alpha^2 \hbar c R_H \left\{ \frac{j(j+1) - l(l+1) - s(s+1)}{2n^3 l(l+\frac{1}{2})(l+1)} \right\}$$



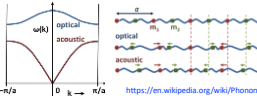
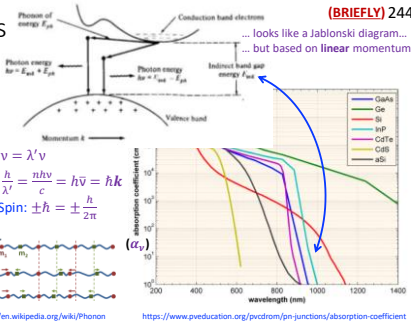
... oh, now I see it in those spectra... and how the black spectrum is when there is a mixture



## E–k Diagrams

(BRIEFLY) 244

**Phonons**  
 Particle Type: Boson  
 Mass: 0  
 Charge: 0  
 Energy:  $E = \hbar \nu = \hbar \omega$   
 Linear Velocity:  $\frac{E}{n} = \left(\frac{\lambda}{n}\right) \nu = \lambda' \nu$   
 Linear Momentum:  $p = \frac{h}{\lambda'} = \frac{n\hbar \nu}{c} = \hbar n \nu = \hbar k$   
 z Angular Momentum / Spin:  $\pm \hbar = \pm \frac{h}{2\pi}$



<https://en.wikipedia.org/wiki/Phonon>

<https://www.pveducation.org/pvcdrom/psn-junctions/absorption-coefficient>

... looks like a Jablonski diagram...  
 ... but based on linear momentum



## Absorption Coefficient & Beer–Lambert Law 245

To describe attenuation of light intensity/power through matter **due to absorption only**... one writes  $\frac{\partial I_v}{\partial z} = -\alpha_v I_v$ ... where  $\alpha_v$  is the linear Napierian **absorption coefficient** ( $\text{cm}^{-1}$ )

Rearranging to  $\frac{\partial I_v}{I_v} = -\alpha_v \partial z$ , and integrating from  $I_{v,front}$  to  $I_{v,back}$  over  $\ell$  leads to...

$$\ln \left( \frac{I_{v,back}}{I_{v,front}} \right) = -\alpha_v \ell \dots \text{ or } I_v = I_{v,0} e^{-\alpha_v \ell}, \text{ where } I_v = I_{v,back} \text{ and } I_{v,0} = I_{v,front}$$

... where  $T_v = \frac{I_{v,back}}{I_{v,0}}$  (transmittance) and  $A_v = -\log(T_v) = \log\left(\frac{I_{v,0}}{I_v}\right)$  (absorbance)

... but the **absorption coefficient** can take on many forms/units... sorry...

$$\log\left(\frac{I_v}{I_{v,0}}\right) = -\alpha_v \ell \dots \text{ where } \alpha_v \text{ is the linear decadic absorption coefficient } (\text{cm}^{-1}) \text{ [not often used]}$$

$$\ln\left(\frac{I_v}{I_{v,0}}\right) = -\kappa_v c \ell \dots \text{ where } \kappa_v \text{ is the molar Napierian absorption coefficient } (\text{M}^{-1} \text{cm}^{-1}) \text{ [n. o. u.]}$$

... since  $\text{M}^{-1} \text{cm}^{-1} = \text{L mol}^{-1} \text{cm}^{-1} = \text{dm}^3 \text{mol}^{-1} \text{cm}^{-1}$ ,  $\sigma_v = \frac{1000000}{N_A}$  is the **absorption cross-section** ( $\text{cm}^2$ )

$$\log\left(\frac{I_v}{I_{v,0}}\right) = -\epsilon_v c \ell \dots \text{ where } \epsilon_v \text{ is the molar decadic absorption coefficient } (\text{M}^{-1} \text{cm}^{-1}) \dots \text{ finally!} \dots$$

... leading to the **Beer–Lambert law**...  $A_v = \epsilon_v c \ell$ ... a succinct and well-known equation in the end

<https://goldbook.iupac.org/terms/view/A00037>





