Consider the electrochemical cell:

$$\operatorname{Ag}_{(S)} |\operatorname{AgCl}_{(S)}|\operatorname{Cl}^{\text{-}} \|\operatorname{Zn}^{2+}|\operatorname{Zn}_{(S)}$$

The Cell Potential  $\mathbf{\mathcal{E}}_{cell}$  can be calculated by two methods:

## **Method 1: Total Reaction Method**

The total cell reaction is:

$$Zn^{2+} + 2Ag_{(s)} + 2Cl^{-} => Zn_{(s)} + 2AgCl_{(s)}$$

$$\mathcal{E}_{\text{cell}} = \mathcal{E}^{\circ}_{\text{cell}} - (RT/2F) \ln (1/([Zn^{2+}][Cl^{-}]^{2}))$$
 (1)

where  $\mathbf{E}^{\circ}_{cell} = -\Delta G^{\circ}/2F$ 

## Method 2: Half Cell Potential Method

$$\varepsilon_{\text{cell}} = \varepsilon_{\text{Zn}} - \varepsilon_{\text{AgCl}}$$
 (2)

$$Zn^{2+} + 2e => Zn_{(s)}$$

$$E_{Zn} = E^{\circ}_{Zn} - (RT/2F) \ln (1/[Zn^{2+}])$$
 (3)

$$AgCl_{(S)} + e = > Ag_{(S)} + Cl^{-}$$

$$E_{AgCl} = E^{\circ}_{AgCl} - (RT/F) \ln ([Cl^{-}])$$
(4)

## **Equivalence of the Two Methods**

Now since (RT/F)  $\ln ([Cl^-]) = -(RT/F) \ln (1/[Cl^-]) = -(RT/2F) \ln (1/[Cl^-]^2)$  this eqn becomes:

$$E_{AgCl} = E^{\circ}_{AgCl} + (RT/2F) \ln (1/[Cl^{-}]^{2})$$
(5)

$$\epsilon_{cell} = (\epsilon_{Zn} - (RT/2F) \ln (1/[Zn^{2+}])) - (\epsilon_{AgCl} + (RT/2F) \ln (1/[Cl^{-}]^{2}))$$
 (6)

$$\mathbf{\epsilon}_{cell} = (\mathbf{E}^{\circ}_{Zn} - \mathbf{E}^{\circ}_{AgCl}) - (RT/2F) \ln (1/([Zn^{2+}][Cl^{-}]^{2})$$
(7)

If we define  $(E^{\circ}_{Zn} - E^{\circ}_{AgCl}) = \mathcal{E}^{\circ}_{cell}$ , Then we see that this is exactly the same equation that we found by Method 1 (Equation 1).